### The Infinite Art of Fractals: Exploring Patterns in Math and Nature

Welcome to the amazing world of fractals! Prepare to see mathematics in a whole new, artistic light.

### What are Fractals? (Approx. 15 minutes)

Have you ever looked closely at a fern leaf and noticed how the whole leaf shape is repeated in its smaller parts? Or how a coastline looks jagged and complex whether you're looking at it from space or up close? These are examples of fractal-like patterns!

A fractal is a never-ending pattern that repeats itself at different scales. This property is called **self-similarity**. Think of it like a set of Russian nesting dolls, where each doll is a smaller version of the one before it, but with fractals, this can go on infinitely!

Key Characteristics of Fractals:

- Self-Similarity: They look similar at different levels of magnification.
- Infinite Detail/Complexity: You can zoom in forever, and new details will emerge.
- Generated by Iteration: They are often created by repeating a simple process over and over again.

# Activity 1: Constructing the Sierpinski Triangle (Approx. 30 minutes)

Let's create one of the most famous fractals!

- 1. Start by drawing a large equilateral triangle on your paper. (An equilateral triangle has all three sides of equal length and all three angles equal to 60 degrees).
- 2. Find the midpoint (the exact middle point) of each side of your triangle.
- 3. Connect these three midpoints. This will form a new, smaller equilateral triangle in the center, pointing downwards.
- 4. Imagine you are 'removing' this central triangle (you can shade it in lightly or leave it blank if you are using an outline). You should now have three smaller equilateral triangles at the corners of your original triangle.
- 5. Now, for each of these three new corner triangles, repeat steps 2-4. That is, find the midpoints of their sides, connect them to form an even smaller central triangle, and 'remove' it.
- 6. Continue this process for at least 2 more iterations (levels). The more you do it, the more detailed your fractal will become!

*Discussion:* What do you observe as you add more iterations? How many black (or unshaded) triangles are there after 1 iteration? 2 iterations? 3 iterations? Can you see a pattern?

### Activity 2: Creating the Koch Snowflake (Side) (Approx. 30 minutes)

The Koch Snowflake is another beautiful fractal. We'll start by creating one side of it, called a Koch curve.

- 1. Draw a straight horizontal line segment. This is 'Iteration 0'.
- 2. Divide this line segment into three equal parts.
- 3. Erase the middle third segment.

- 4. In place of the segment you erased, draw two line segments of the same length as the one you erased, forming an equilateral triangle that points outwards from the original line. This is 'Iteration 1'. You now have a line made of 4 smaller segments.
- 5. Now, for *each* of these four smaller line segments, repeat steps 2-4. (Divide it into thirds, remove the middle, replace it with two sides of an outward-pointing triangle). This is 'Iteration 2'.
- 6. Try to do one more iteration if you can!

*To make a full Koch Snowflake:* Start with a large equilateral triangle. Then, apply the Koch curve process described above to each of the three sides of the initial triangle.

*Discussion:* What happens to the length of the Koch curve as you add more iterations? Does it get longer or shorter? It actually gets infinitely long, even though it encloses a finite area! Cool, right?

## Exploration: Fractals All Around Us! (Approx. 20-30 minutes)

Fractals aren't just mathematical curiosities; they are everywhere in nature and technology!

- **Challenge:** Find and list at least 5 examples of fractal patterns around you (in your home, garden, or by searching online for 'fractals in nature' or 'fractals in technology').
- Some ideas to get you started: Ferns, Romanesco broccoli, snowflakes, coastlines, lightning bolts, tree branches and root systems, river networks, blood vessels and lungs in our bodies, antennas.
- **Optional Online Exploration:** With permission, search for 'online fractal generator' and play with creating digital fractals like the Mandelbrot Set or Julia Sets. See how changing simple mathematical formulas can create incredibly complex and beautiful images.

#### **Creative Application: Design Your Own Fractal-Inspired Art!** (Approx. 45-60 minutes)

Now it's your turn to be a fractal artist!

- 1. Think about the processes you used: starting with a simple shape and repeating a rule to add detail and complexity.
- 2. Brainstorm a simple rule or pattern you could iterate. For example:
  - Start with a square, and at each iteration, add a smaller square to each corner.
  - Start with a circle, and at each iteration, add three smaller circles around its edge.
  - Create your own unique rule!
- 3. Use paper and colored pencils/markers to create your artwork. You can also try sketching it digitally if you prefer.
- 4. Focus on the idea of self-similarity and iteration. Your design doesn't have to be perfectly mathematical, but it should show an understanding of fractal concepts.

Be creative and have fun! Title your artwork and be prepared to explain the 'rule' you used to create it.

#### **Reflection & Sharing (Approx. 15 minutes)**

Let's think about what we've learned:

- What did you find most surprising or interesting about fractals?
- Which fractal did you enjoy creating more, the Sierpinski Triangle or the Koch Snowflake? Why?

- Share your 'Fractal-Inspired Art' and explain the iterative process you used.
- Can you think of any other areas where understanding fractals might be useful (e.g., computer graphics for movies, medicine, engineering)?

#### **Optional Extension Activities:**

- **Research:** Learn about Benoît Mandelbrot, the mathematician often called the 'father of fractal geometry.'
- **Math Dive:** Investigate 'fractal dimension.' Unlike normal shapes (a line has 1 dimension, a square has 2, a cube has 3), fractals can have dimensions that are fractions! For example, the Koch curve has a fractal dimension of about 1.26.
- **Coding (if interested):** Explore creating fractals using simple programming languages like Scratch (using pen blocks and recursion/loops) or Python with the Turtle graphics library.

Great job exploring the infinite world of fractals! You've used math to create art and see the hidden patterns in the world around you.